

Variables and Expressions Guide Notes

VARIABLES are symbols used to represent unspecified numbers or values. Any letter can be used as a variable.

$$x, y, z, a, r, d, s$$

ALGEBRAIC EXPRESSION consists of one or more numbers and variables along with one or more arithmetic operation.

$$6y, 7x - 3, 9 + \frac{r}{s}, k \cdot 5j, 5ab \div 3cd$$

Various ways to represent a product of x and y :

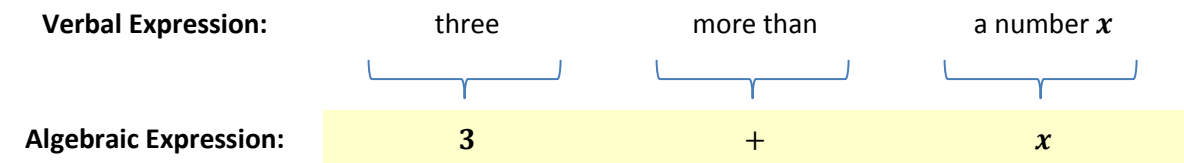
$$xy, x \cdot y, x(y), (x)y, (x)(y)$$

In each expression above, the quantities being multiplied are called **factors**, and the result is called the **product**.

Translating **Verbal Expression** into **Algebraic Expression**:

| Addition | Subtraction | Multiplication | Division |
|-----------------|-----------------------|-----------------------|-----------------|
| Plus | Minus | Times | Divided |
| Sum of | Difference between/of | Product of | Quotient of |
| More than | Less than | Multiplied by | Ratio of |
| Increased by | Decreased by | | Per |
| Combined | Fewer than | | Out of |
| Together | | | percent |
| Total of | | | |
| Added to | | | |

Example: three more than a number x



Sample Problem 1: Write each expression algebraically.

- a. The product of 8 and a number x = **$8x$**
- b. The difference between 16 and x squared = **$16 - x^2$**
- c. The sum of 7 and m = **$7 + m$**
- d. x divided by three = **$\frac{x}{3}$**
- e. Four times eight plus n = **$4(8 + n)$**

POWER is an expression that represents repeated multiplication of the same factor.

$$x^n$$


where: x = base

n = exponent, which corresponds to the number of times the base is used as a factors

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| Symbol | Words | Meaning |
|--------|--------------------------------|---|
| 2^1 | 2 to the first power | 2 |
| 2^2 | 2 to the second power | $2 \cdot 2$ |
| 2^3 | 2 to the third power | $2 \cdot 2 \cdot 2$ |
| 2^4 | 2 to the fourth power | $2 \cdot 2 \cdot 2 \cdot 2$ |
| 2^5 | 2 to the fifth power | $2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$ |
| $2n^6$ | 2 times n to the sixth power | $2 \cdot n \cdot n \cdot n \cdot n \cdot n \cdot n$ |
| x^n | x to the n th power | $x \cdot x \cdot x \cdot x \cdot x \cdot \dots \cdot x$ |

Example: 2^6




| | | | |
|-----------|-------|--|------------|
| Power: | 2^6 | $= 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$ | $2^6 = 64$ |
| Base: | 2 |  | |
| Exponent: | 6 | 6 factors of 2 | |

Sample Problem 2: Find each value.

- a. $3^2 = 3 \cdot 3 = 9$
- b. $4^3 = 4 \cdot 4 \cdot 4 = 64$
- c. $5^2 = 5 \cdot 5 = 25$
- d. $6^2 = 6 \cdot 6 = 36$
- e. $2^4 = 2 \cdot 2 \cdot 2 \cdot 2 = 16$

Translating Algebraic Expression into Verbal Expression:

Example: $4m$

| | | | |
|-----------------------|---|--|---|
| Algebraic Expression: | 4 | · | m |
| |  |  |  |
| Verbal Expression: | four | times | a number m |
| | The product of 4 and m | | |

Sample Problem 3: Write a verbal expression for each algebraic expression.

- a. $3 - t$ = the difference between 3 and t
- b. $y + 9$ = the sum of y and 9
- c. $\frac{6}{s}$ = the ratio between 6 and s
- d. $4z$ = the product of 4 and z
- e. $21d - 3$ = the difference between 21 times d and 3