

Order of Operations and Evaluating Expressions

Guide Notes

EVALUATE ALGEBRAIC EXPRESSIONS means to find its numerical value.

ORDER OF OPERATIONS is a method used to evaluate an expression involving more than one operation. In algebraic expressions, it can only be evaluated if the values of the variables are known.

- Step 1** Replace the variables with their numerical values.
Step 2 Evaluate expressions inside grouping symbols.
Step 3 Evaluate all powers.
Step 4 Do all multiplications and/or divisions from left to right.
Step 5 Do all additions and/or subtractions from left to right.

Example: Evaluate $z^4 - 3$, if $z = 2$.

$$\begin{aligned} z^4 - 3 &= 2^4 - 3 && \text{Replace } z \text{ with } 2. \\ &= 16 - 3 && \text{Evaluate } 2^4 \\ z^4 - 3 &= 13 && \text{Subtract } 16 \text{ and } 3 \end{aligned}$$

Sample Problem 1: Evaluate each expression if $x = 2$, $y = 4$, and $z = 6$.

- a. $x^3 + 10y = 2^3 + 10 \cdot 4 = 8 + 40 = 48$
- b. $\frac{22}{x} + 16 = \frac{22}{2} + 16 = 11 + 16 = 27$
- c. $\frac{z}{3} + y = \frac{6}{3} + 4 = 2 + 4 = 6$
- d. $y + z + x = 4 + 6 + 2 = 12$
- e. $x + 5 = 2 + 5 = 7$

GROUPING SYMBOLS, such as parentheses () or brackets [], indicate the order in which the operations should be performed first.

Example: Evaluate $a^2 - (b^3 - 4c)$, if $a = 8$, $b = 5$, and $c = 3$.

$$\begin{aligned} a^2 - (b^3 - 4c) &= 8^2 - (5^3 - 4 \cdot 3) && \text{Replace } a \text{ with } 8, b \text{ with } 5, \text{ and } c \text{ with } 3. \\ &= 64 - (125 - 4 \cdot 3) && \text{Evaluate } 8^2 \text{ and } 5^3 \\ &= 64 - (125 - 12) && \text{Multiply } 4 \text{ and } 3 \\ &= 64 - 113 && \text{Subtract } 125 \text{ and } 12 \\ a^2 - (b^3 - 4c) &= -49 && \text{Subtract } 64 \text{ from } 113 \end{aligned}$$

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Sample Problem 2: Evaluate each expression if $r = 4$, $s = 6$, $t = 3$, and $u = 12$.

$$f. \quad 2r + st^2 - u = 2(4) + (6)(3^2) - 12 = 8 + 6(9) - 12 = 54 - 4 = 50$$

$$g. \quad tu - rs = (3)(12) - (4)(6) = 36 - 24 = 12$$

$$h. \quad st - 4r = (6)(3) - 4(4) = 18 - 16 = 2$$

$$i. \quad r^3 + u + s^t = 4^3 + 12 + 6^3 = 64 + 12 + 216 = 292$$

$$j. \quad tu - 3r = (3)(12) - 3(4) = 36 - 12 = 24$$

FRACTION BAR is another type of grouping symbol. It indicates that the numerator and denominator should each be treated as a single value.

Example: Evaluate $\frac{x^2-1}{4y^2}$, if $x = 9$, and $y = 2$.

$$\frac{x^2 - 1}{4y^2} = \frac{9^2 - 1}{4 \cdot 2^2}$$

Replace x with 9, and y with 2.

$$= \frac{81 - 1}{4 \cdot 4}$$

Evaluate 9^2 and 2^2

$$= \frac{81 - 1}{16}$$

Multiply 4 and 81

$$= \frac{80}{16}$$

Subtract 81 from 1

$$\frac{x^2 - 1}{4y^2} = 5$$

Divide 80 to 16

Sample Problem 3: Evaluate each expression if $r = 4$, $s = 6$, $t = 3$, and $u = 12$.

$$a. \quad \frac{2r(s-t)}{tu-s} = \frac{2(4)(6-3)}{(3)(12)-6} = \frac{8(3)}{36-6} = \frac{24}{30} = \frac{4}{5}$$

$$b. \quad \frac{u}{s} + \frac{3s}{t^2} = \frac{12}{6} + \frac{3(6)}{3^2} = 2 + \frac{18}{9} = 2 + 2 = 4$$

$$c. \quad \frac{rs^2 - 3u}{2} = \frac{(4)(6^2) - 3(12)}{2} = \frac{4(36) - 36}{2} = \frac{144 - 36}{2} = \frac{108}{2} = 54$$

$$d. \quad \frac{3r+s}{t^2-s} = \frac{3(4)+6}{3^2-6} = \frac{12+6}{9-6} = \frac{18}{3} = 6$$

$$e. \quad \frac{2u+s^2}{r+2t} = \frac{2(12)+6^2}{4+2(3)} = \frac{24+36}{4+6} = \frac{60}{10} = 6$$