Write each expression in radical form.

1.
$$y^{\frac{4}{5}} =$$

2.
$$(4c-3)^{\frac{3}{4}}=$$

Write each expression in exponential form.

3.
$$\sqrt[5]{x^2} =$$

$$4. \qquad \sqrt{(2+a)} =$$

Simplify the following expressions. Assume that all variables represent positive real numbers.

5.
$$\sqrt[4]{81} =$$

$$6. \qquad \sqrt{36a^6b^2} =$$

7.
$$\sqrt{75} =$$

8.
$$\sqrt[4]{\frac{48a^5}{b^8}} =$$

9.
$$\sqrt[4]{162(3x+5)^8} =$$

$$10. \qquad \frac{\sqrt{50x^6}}{\sqrt{2x^4}} =$$

Simplify the following expressions. Assume that all variables represent positive real numbers.

$$\frac{2}{\sqrt{6}} =$$

12.
$$\frac{12}{\sqrt[3]{4}} =$$

13.
$$\frac{3}{10+\sqrt{5}}=$$

$$\frac{y-x}{\sqrt{y}-\sqrt{x}}=$$

Simplify radicals and recognize like or unlike radicals.

15.
$$2\sqrt{3}$$
; $3\sqrt{2}$;

16.
$$3\sqrt{6}$$
; $\sqrt{24}$

17.
$$\sqrt[3]{250}$$
; $\sqrt[3]{54}$; $\sqrt[3]{16}$

18.
$$\sqrt[4]{2a^4b^9}$$
; $6\sqrt[3]{2ab}$; $3\sqrt[4]{2ab^5}$

Simplify the following expressions. Assume that all variables represent positive real numbers.

19.
$$(\sqrt[5]{-32})^2 =$$

$$\sqrt[5]{\sqrt{xy^3}} =$$

ANSWERS

Write each expression in radical form.

1.
$$y^{\frac{4}{5}} = \sqrt[5]{y^4}$$

2.
$$(4c-3)^{\frac{3}{4}} = \sqrt[4]{(4c-3)^3}$$

Write each expression in exponential form.

3.
$$\sqrt[5]{x^2} = \frac{x^2}{x^5}$$

4.
$$\sqrt{(2+a)} = \frac{(2+a)^{\frac{1}{2}}}{(2+a)^{\frac{1}{2}}}$$

Simplify each expression

5.
$$\sqrt[4]{81} = \sqrt[4]{3^4} = +3$$

6.
$$\sqrt{36a^6b^2} = \sqrt{6^2*(a^3)^2*b^2} = \frac{6a^3b}{a^3b^3}$$

7.
$$\sqrt{75} = \sqrt{3 * 5^2} = 5\sqrt{3}$$

8.
$$\sqrt[4]{\frac{48a^5}{b^8}} = \frac{\sqrt[4]{2^4 * 3 * a * a^4}}{\sqrt[4]{b^4b^4}} = \frac{2a\sqrt[4]{3a}}{b^2}$$

9.
$$\sqrt[4]{162(3x+5)^8} = \sqrt[4]{2*3^4*(3x+5)^4*(3x+5)^4} = \sqrt[4]{2*3^4*(3x+5)^2} = \sqrt[4]{2*3^4*(3x+5)^4} = \sqrt[4]{2*3^4*$$

10.
$$\frac{\sqrt{50x^6}}{\sqrt{2x^4}} = \sqrt{\frac{5^2 * 2 * (x^3)^2}{2 * (x^2)^2}} = \frac{5x^3}{x^2} = \frac{5x}{x^2}$$

Simplify the following expressions (rationalize the denominator)

11.
$$\frac{2}{\sqrt{6}} = \frac{2}{\sqrt{6}} * \frac{\sqrt{6}}{\sqrt{6}} = \frac{2\sqrt{6}}{6} = \frac{\frac{\sqrt{6}}{3}}{3}$$

12.
$$\frac{12}{\sqrt[3]{4}} = \frac{12}{\sqrt[3]{4}} * \frac{\sqrt[3]{4^2}}{\sqrt[3]{4^2}} = \frac{12\sqrt[3]{4^2}}{4} = 3\sqrt[3]{2 * 2^3} = \frac{12\sqrt[3]{4^2}}{4} = 3\sqrt[3]{2 * 2^3} = \frac{12\sqrt[3]{4^2}}{4} = \frac{12\sqrt[$$

13.
$$\frac{3}{10 + \sqrt{5}} = \frac{3}{10 + \sqrt{5}} * \frac{10 - \sqrt{5}}{10 - \sqrt{5}} = \frac{3(10 - \sqrt{5})}{10^2 - (\sqrt{5})^2} = \frac{3(10 - \sqrt{5})}{95}$$

14.
$$\frac{y-x}{\sqrt{y}-\sqrt{x}} = \frac{y-x}{\sqrt{y}-\sqrt{x}} * \frac{\sqrt{y}+\sqrt{x}}{\sqrt{y}+\sqrt{x}} =$$
$$= \frac{(y-x)(1+\sqrt{x})}{(\sqrt{y})^2-(\sqrt{x})^2} =$$
$$= \frac{(y-x)(1+\sqrt{x})}{y-x} = \frac{1+\sqrt{x}}{1+\sqrt{x}}$$

Simplify radicals and recognize like or unlike radicals.

15.
$$2\sqrt{3}$$
; $3\sqrt{2}$;

16.
$$3\sqrt{6}$$
; $\sqrt{24}$
 $3\sqrt{6}$; $\sqrt{2^2 * 6}$
 $3\sqrt{6}$; $2\sqrt{6}$

18.

UNLIKE RADICALS

17.
$$\sqrt[3]{250}$$
; $\sqrt[3]{54}$; $\sqrt[3]{16}$
 $\sqrt[3]{2 * 5^3}$; $\sqrt[3]{2 * 3^3}$; $\sqrt[3]{2 * 2^3}$
 $\sqrt[5]{2}$; $\sqrt[3]{2}$; $\sqrt[2]{2}$

LIKE RADICALS

UNLIKE RADICALS

Simplify the following expressions.

19.
$$\left(\sqrt[5]{-32}\right)^2 = \sqrt[5]{(-2)^{5*2}} = \sqrt[5]{(-2)^{10}} = 20.$$
 $\sqrt[5]{\sqrt{xy^3}} = \sqrt[5*2]{xy^3} = \sqrt[10]{xy^3}$ $\sqrt[5*2]{-20}$

$$\sqrt[5]{\sqrt{xy^3}} = \sqrt[5*2]{xy^3} = \sqrt[10]{xy^3}$$